

Modelling early-type stars in eclipsing binaries of open clusters: a new method for age determination from ratio of radii

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Abstract:

Binary systems, in particular eclipsing binaries, are essential sources of our knowledge of the fundamental properties of stars. The ages of binaries, members of open clusters, are constrained by their own fundamental properties and by those of the hosting cluster. The ages of eleven open clusters are here found by constructing models for the components of twelve eclipsing binaries. The difference between the ages we found and the ages of the clusters derived from isochrone fitting is up to 40 %. For the binary system V497 Cep in NGC 7160, the difference is about 100 %. Binary systems whose primary component is about to complete main-sequence life time, such as V453 Cyg and V906 Sco, are the most suitable systems for age determination. Using model results for these stars, we derive an expression for sensitive and uncomplicated relative age determination of binary systems (age divided by the main-sequence life time of the primary star). The expression is given as logarithm of radii ratio divided by a logarithm of mass ratio. Two advantages of this expression are that (i) it is nearly independent of assumed chemical composition of the models because of the appearance of the ratio of radii, and (ii) the ratios of radii and masses are observationally much more precise than their absolute values. We also derive another expression using luminosities rather than radii and compare results.

Keywords: binaries: eclipsing – open clusters – stellar: interior – stellar: evolution

1 Introduction

Nature is full of signals displaying its past and present structure. Astrophysics is extremely specialized in detecting and extracting such signals from very noisy backgrounds. In this context, research on deep regions of stars is a real adventure. Our knowledge of the internal structure and evolution of stars is mostly based on model computations, which take into account and combine outcomes of almost all branches of modern physics. To test how well our stellar models represent real stars, very accurate observational constraints, such as mass, luminosity, radius, chemical composition, and rotational properties, are required. These constraints are obtained from observation of the outer regions, which depend on the physical conditions in the deep interior.

Time is one of the essential components of our universe. Understanding the evolution of the far and near Universe depends on how successful we are in determination of the ages of astrophysical objects. In this respect, every type of age determination is crucial for completing the picture. In this context, we consider the observed detached eclipsing binaries (DEBs) that are members of open clusters, to obtain some basic information pertaining to stars.

In the literature, thirteen well observed DEBs in twelve open clusters are found. Among these systems, V818 Tau in Hyades has already been investigated in detail by the author and his colleagues (Yıldız *et al.* 2006) and is therefore is not included here. Thus, twelve DEBs in eleven open clusters are studied, namely, V453 Cyg in NGC 6871, V1229 Tau (HD 23642) in Pleiades, V578 Mon in NGC 2244, V906 Sco in NGC 6475, V497 Cep in NGC 7160, V381 Car (HD

92024) in NGC 3293, V392 Car in NGC 2516, V1034 Sco in NGC 6231, DW Car in Cr 228, GV Car in NGC 3532, V615 Per and V618 Per in NGC 869. The masses of the binaries vary between $1.54 M_{\odot}$ and $16.84 M_{\odot}$; therefore, this study essentially deals with the structure and evolution of the early-type stars.

The key point for stellar evolution is the increase in mean molecular weight, which causes contraction in nuclear core. The temperature of the core is increased by the heat released as a result of contraction, and hence nuclear reactions are intensified. This is the basic mechanism that controls the evolution and determines the time dependence of stellar structure. By constructing rotating (for the rapidly rotating components of DW Car) and non-rotating evolutionary models for the component stars in the DEBs, we obtain information about the age and chemical composition of the binaries and hence about their clusters. The information about age and chemical composition is deduced by fitting accurate values of luminosities and radii of component stars, if possible. We also obtain some simple expressions based on the slope of mass–radius and mass–luminosity relations for the binaries in order to find the age of binary systems easily.

The ages of stars are derived by means of various astrophysical techniques including (i) observed surface properties (see, for example, Kharchenko *et al.*, 2005; Yıldız *et al.*, 2006); (ii) seismic properties (in particular for the stars with the solar-like oscillations, see for example, Eggenberger *et al.*, 2008; Yıldız 2007, 2008); (iii) rotational properties (Mamajek & Hillenbrand, 2008); and (iv) radioactive elements (del Peloso *et al.*, 2006). The most widely used technique is based on the observed surface properties, which is also the method of the present study.

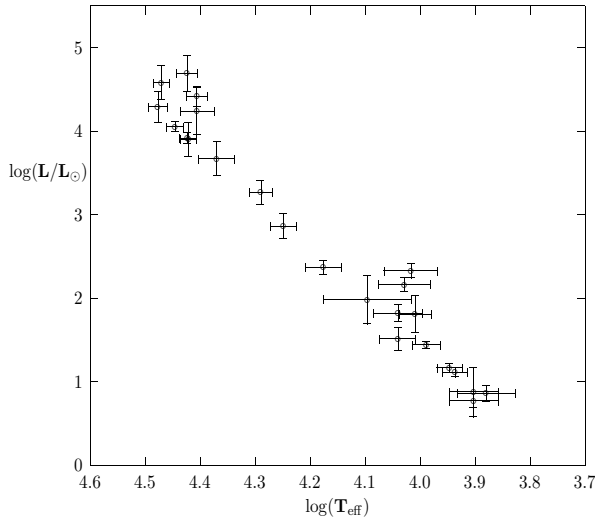


Figure 1: Observational HR diagram for the DEBs in open clusters.

The Sun, with its precise seismic and non-seismic constraints, is the first target to model for an upgraded code describing stellar interiors. The agreement between the solar models and observed constraints gives an idea of the quality of the code. One can obtain the initial hydrogen (X_o) and heavy element (Z_o) abundances and the mixing-length parameter of the Sun from the calibration of solar models, and use them when these quantities are not constrained for any star. In Yıldız (2008), X_o , Z_o and α are found as 0.70975, 0.016 and 1.82, respectively, for the solar model with heavy element mixture of Asplund, Grevesse & Sauval (2005) and with an age of 4.6 Gyr. The details of the code used in the model computations can also be found in Yıldız & Kızıloğlu (1997) and Yıldız (2007, 2008).

The remainder of this paper is organized as follows. In Section 2, we present the observational fundamental properties of the DEBs in open clusters available in the literature. The models of their components are given in Section 3, and the methods of age determination based on the slopes of mass-radius and mass-luminosity relations are presented and discussed in Section 4. Error analysis for age is presented in Section 5. Finally, we list some concluding remarks in Section 6.

2 Observational Data of the Binaries in Open Clusters

Mass transfer obscures the dependence of the fundamental properties of component stars on secondary causes, such as, time, chemical composition, rotation, and magnetic field. Therefore, semi-detached and contact binaries are beyond the scope of the present study. Accordingly, DEBs, member of open clusters, are studied. We have found in the literature studies of twelve

DEBs in eleven open clusters. The observed properties of their component stars are listed in Table 1. The sixth and the seventh columns list the ages of the clusters given in WEBDA database (<http://obswww.unige.ch>) and Kharchenko *et al.* (2005), respectively. For some of the systems, $L = 4\pi R^2 \sigma T_{\text{eff}}^4$ is not satisfied (see Section 3 and Table 3). Fig. 1 shows the observed Hertzsprung-Russell diagram (HRD) for the component stars of these eclipsing binaries. All the stars are either main-sequence (MS) stars or very close to the MS. The mass interval of the stars ranges from 1.54 (GV Car B) to 16.84 M_\odot (V1034 Sco A) and it covers a large part of the MS in the HRD from O-type to F-type stars. The ages of clusters vary between 5 My and 310 My. In the upper part of the MS in Fig. 1, from left to right, the ages of stars increase as theoretically expected. This result shows that the time dependence of effective temperature is more significant than any other second order dependence (e.g., chemical composition, rotation), at least for these stars.

The eleven clusters hosting the studied eclipsing binaries are at distances ranging from 150 (Pleiades) to 2327 pc (NGC3293). Number of stars in the clusters observed by UBV photometry is good enough to estimate the ages of the clusters by isochrone fitting. The WEBDA ages taken from different studies vary. Kharchenko *et al.* (2005) essentially use the isochrones of Girardi *et al.* (2002) for age determination.

These binaries have attracted attention in recent years. None of them is among the well known binaries in Andersen (1991). However, six of them (V453 Cyg, V578 Mon, V906 Sco, V392 Car, V1034 Sco and DW Car) are listed in the recent compilation by Torres *et al.* (2010). Here we shall compare the basic properties of the stars in Table 1 with that of given in Andersen (1991).

The slope of the mass-luminosity relation derived using the data in Table 1 is 3.89. This means that

$$L \propto M^{3.89}. \quad (1)$$

For the same mass range, we find $L \propto M^{4.02}$ for the DEBs with the most precise data on the fundamental properties (Andersen 1991). These two values for the power of M are very close to each other. The slope of the mass-radius relation of the stars in Table 1 is found as 0.704. That is to say $R \propto M^{0.704}$. For the well-known eclipsing binaries (Andersen 1991), we find that $R \propto M^{0.82}$. The slopes we find for the mass-radius and the mass-luminosity relations for binaries given in Table 1 are slightly less than the slopes found from the well known binaries. The reason may be that many stars in the $\log(M/M_\odot)$ interval [0.1,0.4] in Andersen (1991) have larger radii than their terminal-age MS (TAMS) radius. If we take the mass range as [2.5 M_\odot , 16.84 M_\odot] rather than [1.54 M_\odot , 16.84 M_\odot], the slopes of the mass-luminosity and the mass-radius relations for the well known binaries are found as 3.94 and 0.723, respectively. These values are very close to the values we find for the eclipsing binaries in the open clusters.

Table 1: The fundamental properties of the double-lined eclipsing binaries, which are members of open clusters.

Star	M/M_{\odot}	R/R_{\odot}	$\log(Te(K))$	$\log(L/LR_{\odot})$	$t_W(y)$	$t_{Kh}(y)$	Cluster	$P(y)$
V615 Per A	4.075 ± 0.055	2.291 ± 0.141	4.176 ± 0.033	2.370 ± 0.080	1.172×10^7	1.91×10^7	NGC869	1
V615 Per B	3.179 ± 0.051	1.903 ± 0.094	4.041 ± 0.045	1.820 ± 0.100				
V618 Per A	2.332 ± 0.031	1.636 ± 0.069	4.041 ± 0.033	1.510 ± 0.140	1.172×10^7	1.91×10^7	NGC869	1
V618 Per B	1.558 ± 0.025	1.318 ± 0.069	3.903 ± 0.045	0.770 ± 0.080				
V453 Cyg A	14.36 ± 0.20	8.551 ± 0.055	4.424 ± 0.019	4.690 ± 0.210	9.08×10^6	9.77×10^6	NGC6871	1
V453 Cyg B	11.11 ± 0.13	5.489 ± 0.063	4.406 ± 0.031	4.240 ± 0.280				
V1229 Tau A	2.193 ± 0.022	1.831 ± 0.029	3.989 ± 0.026	1.437 ± 0.047	1.5×10^8	1.35×10^8	Pleiades	3
V1229 Tau B	1.550 ± 0.018	1.548 ± 0.044	3.880 ± 0.053	0.858 ± 0.095				
V578 Mon A	14.54 ± 0.08	5.23 ± 0.06	4.477 ± 0.017	4.291 ± 0.188	7.870×10^6	5.01×10^6	NGC2244	4
V578 Mon B	10.29 ± 0.06	4.32 ± 0.07	4.421 ± 0.015	3.901 ± 0.200				
V906 Sco A	3.253 ± 0.069	3.515 ± 0.039	4.029 ± 0.047	2.162 ± 0.082	2.400×10^8	1.66×10^8	NGC6475	1
V906 Sco B	3.378 ± 0.071	4.521 ± 0.035	4.017 ± 0.048	2.330 ± 0.084				
V497 Cep A	6.89 ± 0.46	3.69 ± 0.03	4.290 ± 0.021	3.265 ± 0.144	1.896×10^7	4.57×10^7	NGC7160	6
V497 Cep B	5.39 ± 0.40	2.92 ± 0.03	4.249 ± 0.023	2.860 ± 0.152				
V381 Car A	15.0 ± 3.0	8.4 ± 0.8	4.406 ± 0.020	4.419 ± 0.121	1.032×10^7	8.71×10^6	NGC3293	7
V381 Car B	3.0 ± 0.5	2.1 ± 0.4	4.096 ± 0.080	1.980 ± 0.290				
V392 Car A	1.900 ± 0.02	1.625 ± 0.030	3.947 ± 0.023	1.162 ± 0.055	1.123×10^8	1.20×10^8	NGC2516	8
V392 Car B	1.853 ± 0.02	1.600 ± 0.030	3.937 ± 0.023	1.109 ± 0.056				
V1034 Sco A	16.84 ± 0.48	7.45 ± 0.07	4.471 ± 0.015	4.580 ± 0.200	6.967×10^6	6.46×10^6	NGC6231	9
V1034 Sco B	9.38 ± 0.27	4.18 ± 0.04	4.370 ± 0.033	3.672 ± 0.210				
DW Car A	11.34 ± 0.12	4.558 ± 0.045	4.446 ± 0.016	4.055 ± 0.063	6.761×10^6	4.79×10^6	Cr228	10
DW Car B	10.63 ± 0.14	4.297 ± 0.055	4.423 ± 0.016	3.915 ± 0.067				
GV Car A	2.51 ± 0.03	2.57 ± 0.05	4.009 ± 0.030	1.807 ± 0.219	3.105×10^8	2.82×10^8	NGC3532	11
GV Car B	1.54 ± 0.02	1.43 ± 0.06	3.903 ± 0.045	0.875 ± 0.300				

1) Southworth *et al.* (2004a), 2) Southworth *et al.* (2004b), 3) Southworth *et al.* (2005), 4) Hensberge *et al.* (2000), 5) Alencar *et al.* (1997), 6) Yakut *et al.* (2003), 7) Freyhammer *et al.* (2005), 8) Debernardi & North (2001), 9) Bouzid *et al.* (2005), 10) Southworth & Clausen (2007), 11) Southworth & Clausen (2006)

^{a)} The values given for the luminosities, radii and effective temperatures do not obey the luminosity equation $L = 4\pi R^2 \sigma T_e^4$ (see Section 3 and Table 3).

3 Ages of the Clusters from Models of the Component Stars in the Eclipsing Binaries

The age of a binary system can be found from the solution of two equations based on the coevality of the component stars with two unknowns. One of the equations is written for the difference between the ages of the two components of the binary based on observed luminosities:

$$\Delta t_L = t_{LA} - t_{LB}, \quad (2)$$

where t_{LA} and t_{LB} are ages found from luminosities of primary and secondary components, respectively. The other equation based on the radii:

$$\Delta t_R = t_{RA} - t_{RB}, \quad (3)$$

where t_{RA} and t_{RB} are ages from the radii of primary and secondary components, respectively. From the assumption of coevality, $\Delta t_L = \Delta t_R = 0$. Using numerical derivatives of Δt_L and Δt_R with X and Z , we solve these equations and find X and Z . In general, we find that different combinations of X and Z for a given binary give similar results; thus, the solution is not unique. If it is not possible to obtain an acceptable solution to Eqs. (2) and (3) for a binary system, then we either use one of these equations or fit the model of one of its components to observed values.

In the following subsections, interior models of the component stars in Table 1 constructed using the stellar evolution code described in Yıldız & Kızıloğlu (1997) and Yıldız (2007, 2008) are presented. From these models, the ages and chemical composition of the binaries are obtained if possible.

3.1 On the Fundamental Properties of Components of V615 Per and V618 Per

In this subsection, we consider the binary systems V615 Per and V618 Per in more detail. Their components give very different ages. The reason for this difference should be investigated. For V615 Per, we compare its components with those of V618 Per and find that the luminosity of V615 Per B is lower than is expected for its mass. If we assume that the power of mass is 4 for the slope of the mass–luminosity relation, then $\log(L_B/L_\odot) = 2.02$, which is larger than the value found from observations by amount of 0.2. Since the slope of the mass–radius relation for the components of V615 Per and V618 Per seems reasonable, we deduce that the effective temperature of V615 Per B should be larger than the value found by Southworth, Maxted & Smalley (2004a). As a matter of fact, the results they give for the effective temperatures of V615 Per B ($M_B = 3.18 \pm 0.05 M_\odot$) and V618 Per A ($M_A = 2.33 \pm 0.03 M_\odot$) are the same, despite the very different masses.

Reasonable models for the components of V618 Per are obtained with $Z=0.01$ and $X=0.735$. In the HRD,

the positions of the models at the ages of the cluster given in WEBDA and by Kharchenko *et al.* are the same for V618 Per A. For V618 Per B, the age=19.1 My (Kharchenko *et al.* 2005) is more suitable than 11.7 My (WEBDA). At 11.7 My, V618 Per B is in the pre-MS stage. The ages and the chemical compositions we find are listed in Table 2.

The accurate values of the components of V615 and V618 Per given in Southworth (2004a) do not exactly obey $L = 4\pi R^2 \sigma T_{\text{eff}}^4$. According to Southworth (private communication), this arises because the same distance for the two components of a DEB is enforced in the light-curve analysis. For the system V615 Per, however, the problem is with V615 Per B, particularly with its effective temperature. For its $\log(L/L_\odot) = 1.82$ and $R/R_\odot = 1.903$ values, its effective temperature should be 12000 K rather than 11000 K. The suggested values are given in bold style in Table 3.

For age determination of these systems, we use observational radii of the component stars as constraints for their interior models, because of the complicated luminosities and effective temperatures. The age of these systems is roughly estimated as 20 My. V615 Per B seems to be a MS star at this age.

3.2 On the Fundamental Properties of Components of V906 Sco

The difference between the masses of the components of V906 Sco is not very large but the primary component is a TAMS star and therefore very appropriate for age determination. The ages are found from the solution of Eqs. (2) and (3), based on the coevality of the component stars. We solve these equations and find X and Z . Using different reference models, we obtain very different combinations of X and Z , hence the solution is not unique. However, the ages found from luminosities and radii of V906 Sco A and B are very close to each other. For the three cases given in Table 4, the age found from R_B (the last column) is slightly less than the others. The mean value of ages is 252 My. Without t_{RB} it is 256 My.

3.3 V578 Mon

This system has the lowest values for slopes of the mass–luminosity and the mass–radius relations among the systems with the early-type components:

$$l_m = \log(L_A/L_B)/\log(M_A/M_B) = 2.6, \\ r_m = \log(R_A/R_B)/\log(M_A/M_B) = 0.55.$$

This means that either the observational values of L_A and R_A are very low or the the observational values of L_B and R_B are very high, compared to the values expected for their masses. The influence of this point on the age determination of the system is crucial.

Abundances of some heavy elements (including C, N and O) are found from disentangled spectra by Pavlovski and Hensberge (2005). The oxygen is underabundant by about -0.10 dex. If we take the solar $Z_s = 0.0122$ (surface heavy element abundance), then Z_0 of NGC 2244 is about 0.01.

Table 2: The chemical composition and age of the binary systems derived from the calibration of models. The ages we find are listed in the fourth column. For comparison, the ages of the clusters given in the WEBDA database and by Kharchenko *et al.* (2005) are also presented. The seventh column reports the MS life time of the primary components of the binary systems. In the eighth column, the age found from the ratio of radii of the component stars is shown (see Section 4). The ages found from the fitting formula given in Eqs. 6-9 are listed in ninth column

Star	X	Z	$t(y)$	$t_W(y)$	$t_{Kh}(y)$	t_{MSA}	t_{rm}	t_{rmf}	Cluster
V615 Per	0.7350	0.0100	2×10^7	1.172×10^7	1.91×10^7	1.40×10^8	2.92×10^7	2.71×10^7	NGC 869
V618 Per	0.7350	0.0100	2×10^7	1.172×10^7	1.91×10^7	5.98×10^8	— —	— —	NGC 869
V453 Cyg	0.7046	0.0117	1.05×10^7	9.08×10^6	9.77×10^6	1.18×10^7	9.76×10^6	9.60×10^6	NGC 681
V1229 Tau	0.6946	0.0158	1.93×10^8	1.5×10^8	1.35×10^8	6.88×10^8	1.24×10^8	1.44×10^8	Pleiades
V578 Mon	0.7098	0.0160	3.50×10^6	7.870×10^6	5.01×10^6	1.29×10^7	— —	— —	NGC 224
V906 Sco	0.7200	0.0170	2.52×10^8	2.400×10^8	1.66×10^8	2.53×10^8	2.53×10^8	2.53×10^8	NGC 647
V497 Cep	0.7440	0.0125	2.30×10^7	1.896×10^7	4.57×10^7	4.95×10^7	2.17×10^7	2.03×10^7	NGC 710
V381 Car	0.7380	0.0258	1.05×10^7	1.032×10^7	8.71×10^6	1.37×10^7	1.05×10^7	0.43×10^7	NGC 329
V392 Car	0.6837	0.0178	1.23×10^8	1.123×10^8	1.20×10^8	1.04×10^9	1.41×10^8	3.01×10^8	NGC 252
V1034 Sco	0.6961	0.0226	5.51×10^6	6.967×10^6	6.46×10^6	1.02×10^6	5.36×10^6	4.21×10^6	NGC 623
DW Car	0.6934	0.0106	5.22×10^6	6.761×10^6	4.79×10^6	1.56×10^7	4.88×10^6	5.72×10^6	Cr 228
" (Rotat.)	0.6951	0.0078	5.29×10^6	6.761×10^6	4.79×10^6	1.52×10^7	4.75×10^6	5.75×10^6	Cr 228
GV Car	0.7046	0.0104	3.22×10^8	3.105×10^8	2.82×10^8	4.22×10^8	3.21×10^8	3.04×10^8	NGC 353

Table 3: The modifications in the fundamental properties of the double lined eclipsing binaries due to inconsistent results given in the literature are presented in bold style

Star	M/M_\odot	R/R_\odot	$\log T_{\text{eff}}(\text{K})$	$\log(L/L_\odot)$
V615 Per A	4.075 ± 0.055	2.291 ± 0.141	4.176 ± 0.033	2.370 ± 0.080
V615 Per B	3.179 ± 0.051	1.903 ± 0.094	4.079 ± 0.045	1.820 ± 0.100
V618 Per A	2.332 ± 0.031	1.636 ± 0.069	4.041 ± 0.033	1.546 ± 0.140
V618 Per B	1.558 ± 0.025	1.318 ± 0.069	3.903 ± 0.045	0.805 ± 0.080
V453 Cyg A	14.36 ± 0.20	8.551 ± 0.055	4.424 ± 0.019	4.513 ± 0.210
V453 Cyg B	11.11 ± 0.13	5.489 ± 0.063	4.406 ± 0.031	4.056 ± 0.280
V497 Cep A	6.89 ± 0.46	3.69 ± 0.03	4.290 ± 0.021	3.245 ± 0.144
V497 Cep B	5.39 ± 0.40	2.92 ± 0.03	4.249 ± 0.023	2.877 ± 0.152

Table 4: Ages derived from fitting luminosities (t_L) and radii (t_R) of models for V906 Sco A and B to the observed values, for different combinations of hydrogen and heavy element abundances. While the mean of all values is 252 My, the mean value of t_{LA} , t_{LB} and t_{RA} is 256 My.

X	Z	$t_{LA}(\text{My})$	$t_{LB}(\text{My})$	$t_{RA}(\text{My})$	$t_{RB}(\text{My})$
0.720	0.0170	256	256	253	235
0.729	0.0156	256	259	258	240
0.737	0.0142	257	260	253	244

From the models of the component stars with solar composition ($X_o = 0.70975$, $Z_o = 0.016$), we find the agreement time for the quantities L_A , L_B , R_A , and R_B . While t_{LA} and t_{RA} are about 3.5 My, t_{LB} and t_{RB} are about three and two times larger than 3.5 My, respectively. The reason for the small radius of V578 Mon A or large radius of V578 Mon B may be the accuracy of the data. However, if this is not the case then this system has some interesting features which are beyond the standard models, for example, existence of rapidly rotating core for V578 Mon A (Yıldız 2003, 2005) or rotational mixing (Meynet & Maeder 2000). Within the standard approach, the present data implies that V578 Mon B is more *evolved* than V578 Mon A. The compatible radius for V578 Mon A based to its mass is about $6 R_\odot$, which is 15 % larger than the observed value. Assuming the same effective temperature as given by Hensberge *et al.* (2000), the increase in luminosity of V578 Mon A due to the increase in its radius is about 30 %. For this radius and luminosity, the age of the system is found as 6 My from the models of V578 Mon A and B with $Z=0.01$ and $X=0.710$.

Hensberge *et al.* (2000) shows that the position of V578 Mon A in HRD corresponds to $11 M_\odot$. This may be a manifestation of the rapidly rotating cores of early type stars.

3.4 V392 Car

The masses of the components of V392 Car are very close to each other: $M_A = 1.90 \pm 0.02 M_\odot$, $M_B = 1.853 \pm 0.02 M_\odot$ (Debernardi & North 2001). In Table 5, the ages found from the luminosities and radii for different combinations of X and Z are listed. For such systems with similar components, small differences due to uncertainties in the observed quantities may lead very different results in model computations. However, the observed values of the radii of the component stars are very accurate and provide an opportunity to determine the age of the system very accurately. The models with $X = 0.6837$ and $Z = 0.0178$ predict very close ages for V392 Car A and B (126 and 122 My, respectively). The adopted value for the age, 124 My, is the mean of these values. Debernardi & North (2001) reported very similar metallicity for V392 Car, $Z=0.018$, using evolutionary tracks of Schaller *et al.* (1992).

3.5 V1229 Tau (HD 23642)

The fundamental properties of components of V1229 Tau are determined from light and radial velocity curves by Munari *et al.* (2004), Southworth *et al.* (2005) and Groenewegen *et al.* (2007). The results of these studies are very similar. Among the eclipsing binaries in open clusters considered, this system has the minimum value of

$$r_m = \log(R_A/R_B)/\log(M_A/M_B).$$

It is not possible to fit models of V1229 Tau A and B to the observed properties simultaneously. Therefore, we find age of the system by considering V1229 Tau A and B separately.

The age derived from the calibration of V1229 Tau A is 193 My for $(X, Z) = (0.6946, 0.01575)$ and 222 My for $(X, Z) = (0.7104, 0.014)$. However, the age derived from the calibration of V1229 Tau B is 730 My for $(X, Z)=(0.7046, 0.01305)$. This value is about five times greater than the value given by Kharchenko *et al.* In comparison to the age found for V1229 Tau B, the ages found for V1229 Tau A are close to the ages of Kharchenko *et al.* Southworth *et al.* (2005) finds an age about 125-175 My, close to the results from the calibration of V1229 Tau A. The age of V1229 Tau is listed as 193 My in Table 2.

3.6 V453 Cyg

Recently, precise fundamental properties of V453 Cyg A and B have been presented by Southworth, Maxted & Smalley (2004b). However, there is a contradiction in their results. According to the radii and effective temperatures of the components, the luminosities must be lower than the published values; in their Table 11, they give $\log(L_A/L_\odot) = 4.69$ and $\log(L_B/L_\odot)=4.24$ but we compute the luminosities from the radii and effective temperatures given in that table and find that $\log(L_A/L_\odot) = 4.513$ and $\log(L_B/L_\odot)=4.056$. The correction in $\log(L)$ is about 0.18; about 50% (see Table 3).

From the calibration of model radii of V453 Cyg A and B for $X=0.700$, we find the age of the system as 10.3 My and $Z=0.0174$. For $X=0.7046$, however, the age and Z are computed as 10.5 My and 0.0117, respectively. Whereas the ages found with very different chemical compositions are very close, the model luminosities with the latter values are in perfect agreement with the (corrected) values found from observations. Southworth, Maxted & Smalley (2004b) give the age of the system as 10 My. The ages determined for V453 Cyg are in good agreement with this age and the age of the cluster given by Kharchenko *et al.* (2005). Such a good agreement is based on the fact that V453 Cyg A is very close to the TAMS.

Abundance analysis of V453 Cyg A and B is made by Pavlovski & Southworth (2009). They found that N, O and Mg abundances for V453 Cyg A are nearly solar and C, Si and Al are underabundant. Regarding the fact that O is the most abundant heavy element for *normal* stars, we estimate that $Z \simeq 0.01$ from oxygen abundance (-0.08 dex) estimated by Pavlovski & Southworth (2009). This value is in good agreement with the values predicted from the models ($Z=0.0117$). Pavlovski & Southworth also re-derived the effective temperatures of V453 Cyg A and B: $T_{\text{effA}} = 27,900 \pm 400$ K and $T_{\text{effB}} = 26,200 \pm 500$ K. These values are 5 and 3% greater than the values given by Southworth, Maxted & Smalley (2004b).

Pavlovski & Southworth forecast the helium abundance as 0.086 and 0.123 dex, depending upon the method for derivation of microturbulence velocity. For these helium abundances, very similar ages are found: for 0.086 dex, $Z=0.0113$ and the mean age is 10 My; for 0.123 dex, $Z=0.0163$ and the mean age is 9 My.

Table 5: Ages derived from fitting the luminosities (t_L) and radii (t_R) of models for V392 Car A and B to the observed values, for different combinations of hydrogen and heavy element abundances

X	Z	$t_{LA}(My)$	$t_{LB}(My)$	$t_{RA}(My)$	$t_{RB}(My)$
0.7200	0.0135	260	200	273	284
0.7020	0.0155	200	156	189	203
0.6900	0.0174	220	182	140	156
0.6837	0.0178	157	98	126	122
0.6825	0.0180	163	101	119	116
0.6880	0.0184	246	182	112	105
0.6800	0.0184	165	99	111	102

3.7 V497 Cep

The fundamental properties of this system were obtained by Yakut *et al.* (2003). Using their findings, the best agreement between the models and the observational results from photometric and spectroscopic analysis is reached with $X=0.744$ and $Z=0.0125$. The derived age 23.0 My is the average of $t_{LA} = t_{RA} = 22.3$ My, $t_{LB}=24.9$ My, and $t_{RB}=22.5$ My. Whereas the age we find is close to the age for the cluster given in WEBDA, it is half of the value derived by Kharchenko *et al.* (2005).

The accurate values given in Yakut *et al.* (2003) do not exactly obey $L = 4\pi R^2 \sigma T_e^4$. It is not easy to find the source of this inconsistency. However, it may be due to round off.

3.8 V381 Car (HD 92024)

V381 Car A is a β Cep for which three oscillation frequencies are observed with $l=2$ and 4 (Freyhammer *et al.*, 2006). Despite the large uncertainty in the fundamental properties of its components (Freyhammer *et al.*, 2005), it is a normal system with its slopes for the mass–radius and mass–luminosity relations given as 0.861 and 3.4894. From the fit of model radii and luminosities to the observed values, with $X=0.738$ and $Z=0.0258$, we find that $t_{LA} = t_{RA} = 10.8$ My and $t_{RB}=9.8$ My. The age of the system is found as 10.5 My, the average of these values. This age is in agreement with the age range (10–13 My) estimated by Freyhammer *et al.* (2005).

The chemical composition found from fitting interior models of V381 Car A and B is very different from that of the other binaries in the sense that both of X and Z are greater than the solar values. This may be a result of the over-estimated masses of V381 Car A and B.

3.9 V1034 Sco

It is a normal system with its slopes for the mass–radius and mass–luminosity relations of 0.9876 and 3.5728, respectively. From the fit of model radii and luminosities to the observed values, with $X=0.6961$ and $Z=0.02255$, we find that $t_{RA} = t_{RB} = 5.64$ My, $t_{LA}=5.72$ My and $t_{LB}=5.05$ My. The age of the system is computed as 5.51 My by taking average of these values. Bouzid *et al.* (2005) confirm that the age of

the system is about 5 My, in good agreement with the findings of the present study.

3.10 DW Car

At first sight, this system seems a normal system with slopes for the mass–radius and mass–luminosity relations of 0.9120 and 4.9858, respectively (Southworth & Clausen, 2007). According to the radii, the components of DW Car are unevolved MS stars and very close the zero-age MS (ZAMS). However, the luminosity derived from the observation implies that DW Car A is an evolved MS star. No simultaneous solution is available for the luminosities of DW Car A and B. From their radii, the age of the system is calculated as 5.22 My. The non-rotating models giving this age are constructed with $X=0.6934$ and $Z=0.01063$. However, DW Car A and B are fast rotators; $v_{eqA} = 182 \pm 3$ km s⁻¹ and $v_{eqB} = 177 \pm 3$ km s⁻¹. Therefore, models rotating like a solid body are also constructed for them. The calibration of rotating models results in nearly the same age, 5.31 My. The hydrogen and metal abundances for the rotating models are $X=0.6951$ and $Z=0.0078$, very close to that of non-rotating models. Southworth & Clausen (2007) reported similar results: about 6 My, $Z \simeq 0.01$.

3.11 GV Car

This system consists of two metallic-line stars and it shows apsidal motion. From the calibration of models of the components, with $X=0.7046$ and $Z=0.0104$, we estimate that $t_{RA} = 324$ My, $t_{RB} = 372$ My, $t_{LA} = 295$ My and $t_{LB}=302$ My. The age of the system is found as 322 My. Southworth & Clausen (2006) give a very similar age for GV Car, 360 My.

4 Mass and Time Dependence of the Mass–radius and the Mass–luminosity Relations

The luminosity and radius of a non-rotating star are function of its mass, chemical composition (X and Z), and age:

$$L = L(M, X, Z, t), \quad R = R(M, X, Z, t).$$

Changes in X and Z shift the evolutionary track of a model for a given mass in HRD. Despite the varia-

Table 6: Luminosity and radius difference between ZAMS and TAMS for evolutionary tracks of V906 Sco A. $\Delta \log(L) = (L_{\text{TAMS}} - L_{\text{ZAMS}})/L_{\text{TAMS}}$, $\Delta \log(R) = (R_{\text{TAMS}} - R_{\text{ZAMS}})/R_{\text{TAMS}}$

Star	X	Z	$\Delta \log(L)$	$\Delta \log(R)$
V906 Sco A	0.702	0.0210	0.458	0.439
	0.720	0.0170	0.456	0.444
	0.729	0.0156	0.457	0.448
	0.737	0.0142	0.456	0.446
GV Car A	0.705	0.0200	0.431	0.422
	0.720	0.0100	0.442	0.423

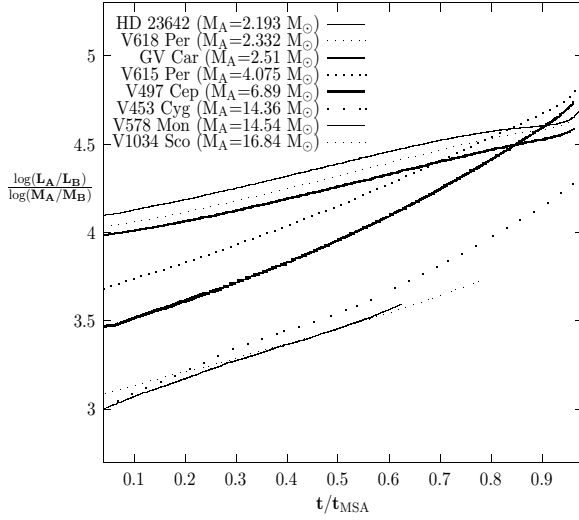


Figure 2: The mass–luminosity relation for the DEBs in open clusters is plotted with respect to the relative age of the primary components.

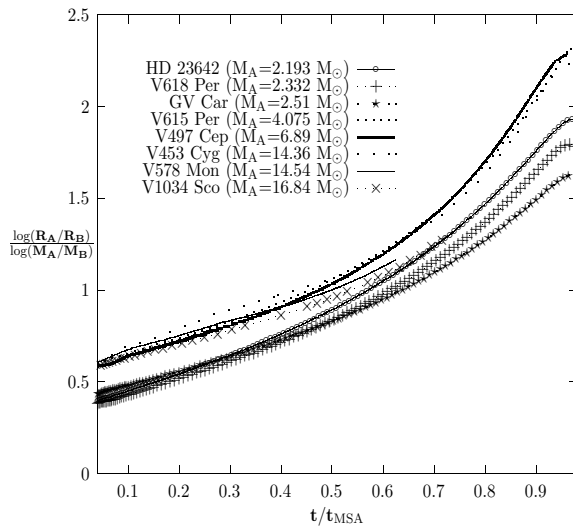


Figure 3: The mass–radius relation for the DEBs in open clusters.

tion in positions of ZAMS and TAMS points according to chosen values of X and Z, ratio of TAMS to ZAMS luminosity is independent of X, Z and stellar mass: the logarithmic luminosity difference, $\Delta \log(L) = (L_{\text{TAMS}} - L_{\text{ZAMS}})/L_{\text{TAMS}}$, is constant. In Table 6, $\Delta \log(L)$ and $\Delta \log(R)$ for the models of V906 Sco A and GV Car A are given in the fourth and the fifth columns, respectively. For very different combinations of X and Z, the differences are between 0.42 and 0.46: the ZAMS luminosity (radius) is about 44 % less than the TAMS luminosity (radius), at least for the early-type stars. Consider a binary system whose component masses are very different, so that the massive component is near the TAMS and the low-mass is still near the ZAMS. For such a system, the luminosity ratio (L_A/L_B) is at a maximum. It was at a minimum when both of the components were near the ZAMS, and gradually increased with time. This is the case also for the ratio of the radii of the components. In this section, we discuss variations of radii and luminosity ratios with time and then develop two methods for age determination of eclipsing binaries.

As stated above, the mass–luminosity relation is not constant and mainly depends on the stellar mass and it increases with time. In Fig. 2, the luminosity–mass ratio ($l_m = \log(L_A/L_B)/\log(M_A/M_B)$) obtained from the models with values given in Table 2 is plotted with respect to the relative age in MS (t/t_{MSA}). Whereas l_m increases with time, there is an inverse relation between l_m and M_A . Near the ZAMS, l_m varies between 3 and 4 and takes values between 4 and 5 near the TAMS. In principle, l_m is very useful for predicting the age of a system if its accuracy is good enough.

The MS life time of the primary stars t_{MSA} , given in the seventh column of Table 2, is mainly a function of M_A , despite very different chemical composition found for the DEBs. From a fit to the M_A – t_{MSA} relation we find that

$$t_{\text{MS}} = \frac{3.37 \times 10^9}{(M/M_{\odot})^{2.122}}. \quad (4)$$

4.1 Age Determination from the Slope of the Mass–radius Relation

The slope of the mass–radius relation $r_m = \log(R_A/R_B)/\log(M_A/M_B)$ is also a function of the primary mass and time. In Fig. 3, r_m is plotted with respect to t/t_{MSA} . From the curves in Fig. 3,

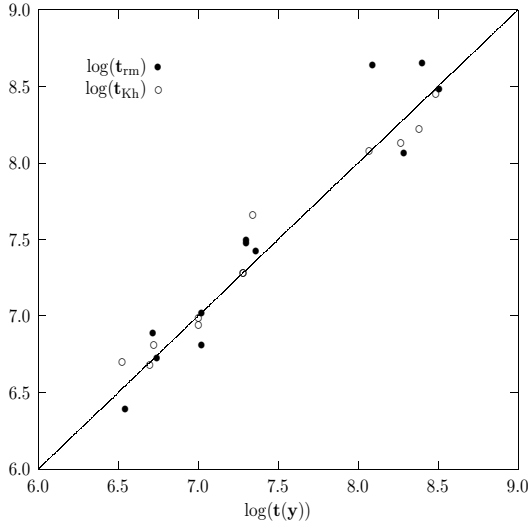


Figure 4: The ages of binaries derived from the ratio of radii (filled circle) are plotted with respect to the ages found from fitting models. For comparison, ages given by Kharchenko *et al.* (2005) are also shown (circle).

we determine the relative age of the binary systems by using the observed values of r_m . Multiplication of relative age of the primary component of a binary system by t_{MSA} gives us age of that binary. The ages (t_{rm}) of all the binaries computed with this method are listed in the eighth column of Table 2. In Fig. 4, these ages (filled circles) are plotted with respect to the ages from fitting interior models of component stars to the observed accurate values (the fifth column in Table 2). For comparison, the ages found by Kharchenko *et al.* (2005) are also shown (circle). There is in general a good agreement between the ages, except for V618 Per and V578 Mon. The observed value of r_m is very high for V618 Per and low for V578 Mon, in comparison with the model values. For V578 Mon, Garcia *et al.* (2010) report that they find a different value for the secondary radius. The difference may significantly influence the observed value of r_m .

The age of V1229 Tau is computed as 124 My by using r_m from Munari *et al.* (2004). r_m from Southworth *et al.* (2005) gives age of the system as 97 My.

The precision of the ages found from the mass-radius curves depends on how sensitive the relative age is to chemical composition. In Fig. 5, r_m s derived from models of V618 Per A and B with different chemical compositions are plotted with respect to the relative age t/t_{MSA} . For $X=0.705$, there is a perfect agreement between r_m s of models with $Z=0.01$ (thin solid line) and $Z=0.02$ (dotted line). We shall also compare r_m values of models with the same Z but different X . r_m of models with $X=0.735$ and $Z=0.01$ (thick solid line) is slightly less than that of the models with $X=0.705$ and $Z=0.01$. The agreement between the three curves of r_m is good enough to suggest that relation between

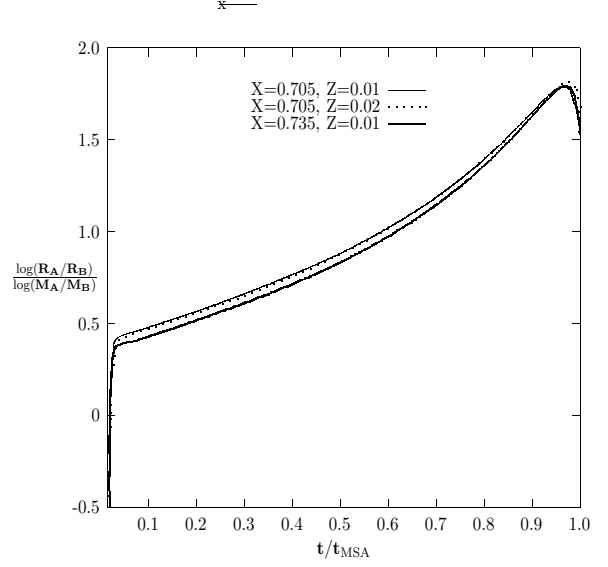


Figure 5: The mass-radius relation for models of V618 Per with different X and Z .

r_m and relative age relation is almost independent of chemical composition. For the precision of the ages, the sensitivity of t_{MSA} to chemical composition is also important. As given in Eq. 4, t_{MSA} is a very strong function of stellar mass. The secondary effect of Z on t_{MSA} behaves as $t_{\text{MSA}} \propto (Z/0.015)^{0.43}$ and is neglected in the present study.

4.2 Simple Expressions for the r_m -age Relation

The time dependence of r_m of binary systems with very different masses and chemical compositions is very similar and therefore can be used to estimate the age of a binary system. To do this, the time variation of r_m is fitted with an equation of the form

$$r_m = a(t/t_{\text{MSA}})^n + b. \quad (5)$$

According to M_A of the binaries, the curves of r_m in Fig. 3 separate essentially into two groups. The r_m values of the binaries with $M_A < 3.4 M_\odot$ take place in the lower part, and those with $M_A > 3.4 M_\odot$ appear in the upper part of Fig. 3. Near the ZAMS of the primary component, r_m is about 0.4 for $M_A < 3.4 M_\odot$ and 0.6 for M_A greater than $3.4 M_\odot$. It increases with time and reaches a value between 1.6 and 2.4. It seems that r_m is a better indicator of binary system age than t_m . For example, age of a system with $r_m = 1$ is about half of the TAMS age of the primary component. For more accurate ages, two fits for the two mass ranges are made to the curves in Fig. 3.

4.2.1 DEBs with Relatively Low-mass Primary Component ($M_A < 3.4 M_\odot$)

In order to increase the precision of Eq. (5), we derive two expressions for low and high values of r_m .

For the three binary systems with $M_A < 3.4M_\odot$, namely, V618 Per, V1229 Tau (HD23642) and GV Car, three separate fits are made to the curves in Fig. 3 by using Eq. 5. Then, the mean values of the parameters (a , b and n) given in Eq. 5 yield

$$\frac{t}{t_{\text{MSA}}} = 0.941(r_m - 0.39)^{0.814} \quad \text{for } r_m < 1.0 \quad (6)$$

and

$$\frac{t}{t_{\text{MSA}}} = 0.77(r_m - 0.588)^{0.431} \quad \text{for } r_m > 1.0. \quad (7)$$

The ages of V1229 Tau and GV Car computed from these expressions (t_{rmf}) are given in the ninth column of Table 2. They are in good agreement with the ages found by other methods.

4.2.2 DEBs with Relatively High-mass Primary Component ($M_A > 3.4M_\odot$)

Using Eq. 5, two fits are applied to the curves of V615 Per, V497 Cep and V453 Cyg given in Fig. 3 according to the value of r_m . We compute the average values of the parameters a , b and n . From these values, the expressions for age as a function of r_m are obtained:

$$\frac{t}{t_{\text{MSA}}} = 1.011(r_m - 0.561)^{0.995} \quad \text{for } r_m < 1.0 \quad (8)$$

and

$$\frac{t}{t_{\text{MSA}}} = 0.613(r_m - 0.852)^{0.330} \quad \text{for } r_m > 1.0. \quad (9)$$

For V615 Per, $r_m = 0.747$ and Eq. (8) gives its age as 27.1 My. These two expressions are used to determine age of the binary systems whose M_A greater than $3.4 M_\odot$ (see Table 2).

The fitting formula given in Eqs. 6-8 are not valid for V381 Car because of the large mass difference between its components. They are also not applicable to binaries with very similar components. For V392 Car, for example, the mass (2.47%) and radius (1.54%) differences between its components are so low that the fitting formula gives an age two times greater than the ages found by other methods. The situation for DW Car is better than V392 Car. The mass (6.26%) and radius (5.73%) differences between the components of DW Car are big enough to predict a reasonable value for age. For V906 Sco, however, there is a big difference between the radii of the components which gives so great value for r_m that we deduce that the age is about $t_{\text{rmf}} = t_{\text{MSA}} = 253\text{My}$.

The r_m curve of V1034 Sco (\times in Fig. 3), which has the highest primary mass ($M_A = 16.84M_\odot$) of the stars studied, is slightly different from the rest. It is in the upper part during the early MS phase as that of the other binaries with $M_A > 3.4 M_\odot$, and joins later on the curves for binaries with $M_A < 3.4 M_\odot$. Therefore, the expressions given in Eqs. 6-7 should be used rather than Eqs. 8-9 for $M_A > 15 M_\odot$ when the relative age is greater than 0.5.

The new expressions proposed above were additionally tested for selected eclipsing binaries. The age

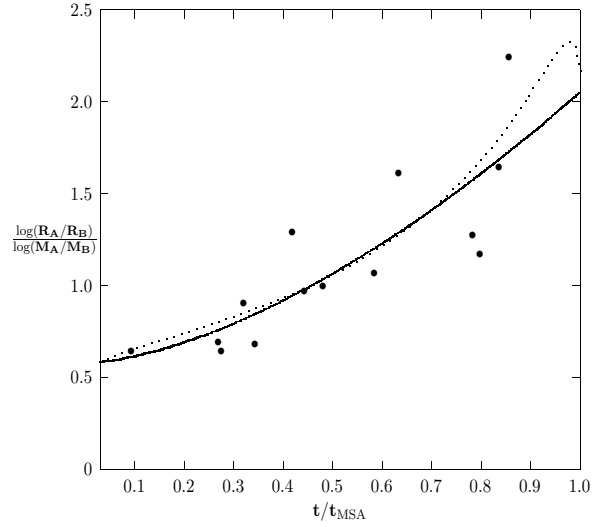


Figure 6: The mass–radius relation for the DEBs given in Andersen (1991) with respect to the relative age of the primary components. The ages are taken from Pols et al. (1997). The solid line is for the curve fitted to this data by using Eq. 5. For comparison, r_m of V497 Cep from models (dotted line) is also plotted.

of HD 42401 is given by Williams (2009) as 25 My and we find the same age (25.6 My) from the ratio of radii. For the age of V539 Ara Clausen *et al.* (1996) and Lastennet and Valls-Gabaud (2002) give 45 and 39 My, respectively. The ratio of radii gives the age as 40.0 My.

4.3 Age Determination from the Slope of the Mass–luminosity Relation

We also derive an expression to determine age from the ratio of luminosities:

$$t = 0.794(l_m - 4.535M_A^{-0.154})10^{(\log M_A - 0.9)^2} t_{\text{MSA}}. \quad (10)$$

This expression gives acceptable ages for only the five binary systems (V453 Cyg, V497 Cep, V381 Car, V1034 Sco and GV Car). The reasons might be that the ratio of luminosities of component stars derived from the light curve of a binary system may not be as accurate as the ratio of radii. The dependence of l_m on M_A is also as important as its time dependence (see Fig. 2).

4.4 Does an r_m –relative Age Relation Implicitly Exist in the Literature?

The time dependence of r_m is not considered in the previous studies in the literature. However, this dependence also exists in Pols et al. (1997), for example, though the authors are not aware of it. In Fig. 6, r_m is plotted with respect to the ages they find (in

units of MS lifetime of the primary components) for the well known binaries (Andersen 1991). In order to avoid complications, the binaries with $M_A > 1.5$ and significantly different components (difference between masses of the components is greater than 10%) are considered. The mass range is 1.56-9.245 M_\odot . The solid line shows the fitted curve for this data using Eq. 5. The dotted line represents the r_m of V497 Cep, already plotted in Fig. 3. The agreement between the two curves is amazing.

5 The Uncertainty in the Ages of the Binaries

The ages of stars we have found involve many uncertainties, based on the model ingredients (e.g., opacity, nuclear reaction rates, equation of state) and the observational quantities. It is very difficult to compute the uncertainty due to the former and therefore we take care in calculating the uncertainties resulting from the latter in our error analysis. The uncertainty in the ages (Δt) derived from the luminosities and radii of component stars is the time interval in which evolutionary tracks of both components stay within the corresponding error boxes in luminosity-radius (L-R) diagram. The values of Δt for the binaries are given in the third column of Table 7. For a binary system whose age is derived from its primary component, the uncertainty is also computed from that star. Within the context of our approach, the uncertainties are reasonably small.

We also compute uncertainties for the ages (Δt_{rm}) derived from the ratio of the radii ($r_{AB} = R_A/R_B$). The uncertainty in the mass ratio appearing in the denominator of r_{rm} is usually very small for well-measured binary systems. The values of Δr_{AB} are available in the literature and given in the fifth column of Table 7. The error in age due to uncertainty in the ratio of the radii is given in the seventh column of Table 7. The uncertainty in the relative age ($\Delta t_{rel} = \Delta t/t_{MSA}$) derived from the ratio of the radii ($r_{AB} = R_A/R_B$) is computed using

$$\Delta t_{rel} = \frac{\Delta r_{AB}}{(\partial r_{AB}/\partial t_{rel})}. \quad (11)$$

The derivative of the ratio of radii with respect to the relative age in Eq. 11 is obtained from the models around the relative age of each binary system. As the masses of component stars are close to each other the derivative is negligibly small and therefore the uncertainty in age is very large. This is the case for the binary systems whose components are very similar: V906 Sco, V392 Car and DW Car. Except V615, the rest of the binary systems have very small uncertainties for their ages. For V615 Per, the reason for the large uncertainty is the large value of Δr_{AB} .

6 Conclusions

Our current understanding of the evolution of our far and near universe depends on accurate age estimates

for astrophysical systems. The stars are the main constituents of these systems, whose ages are essentially determined from comparison of their observed and model properties. Rotating (for DW Car A and B) and non-rotating models for the components of the eclipsing binaries, members of open clusters, are constructed to derive the ages and chemical compositions of the binaries and hence the clusters. The largest difference between the ages we found for the eclipsing binaries and the ages given by Kharchenko *et al.* (2005) for the clusters occurs for the V497 Cep binary system in NGC 7160, where the difference is about 100 %. For the remaining systems the difference is less than 40%.

The binary systems such as V906 Sco in NGC 6475 and V453 Cyg in NGC 6871 are the most suitable systems for age determination: their primary components are about to complete their MS life time and the secondary components are near or not far from the ZAMS. For such systems, despite equivalent solutions with very different chemical compositions, the ages are very close. For the three different solutions with metallicity 0.014-0.017, the age of V906 Sco is in the range 252-254 My.

The slope of the mass-luminosity relation for a binary system depends on mass of its primary component M_A , if M_A is less than about 10 M_\odot . The value of $l_m = \log(L_A/L_B)/\log(M_A/M_B)$ near the ZAMS is 4 for $M_A=2.5 M_\odot$, 3.5 for $M_A=6.89 M_\odot$ and it drops to a minimum value of 3 for $M_A=10 M_\odot$. For binary systems with M_A greater than 10 M_\odot , $l_m = 3$ near the ZAMS and reaches to 4.3 near the TAMS age of their primary component.

The slope of the mass-radius relation changes with time more meaningfully than the slope of the mass-luminosity relation, so is more suitable for estimating the age of the system once it is calibrated. If $r_m=1$ for a system, its age is about half of the MS lifetime of its primary (massive) component. We have derived simple expressions to estimate the age of a binary system from the slope of mass-radius and mass-luminosity relations. In particular, the expressions for the slope of mass-radius relation give very reasonable results (t_{rm}). Eqs.(6)-(9) can be used to predict age of any binary system if the radii and masses of its components are known. The new expressions are tested for the eclipsing binaries HD 42401 and V539 Ara and give excellent results for their ages. The advantage of these expressions for the relative age (t/t_{MSA}) is that they are independent of chemical composition.

Acknowledgments

This work is supported by the Scientific and Technological Research Council of Turkey (TÜBİTAK).

References

- [1] Alencar, S.H.P., Vaz, L.P.R. & Helt, B.E., 1997, A&A, 326, 709
- [2] Andersen, J., 1991, A&AR, 3, 91

Table 7: The uncertainties in the ages of the binaries derived from the error boxes in the luminosity-radius diagram and the uncertainties in the ratio of the radii of the components.

<i>Star</i>	$t(y)$	$\Delta t(y)$	$t_{\text{rm}}(y)$	Δr_{AB}	Δt_{rel}	$\Delta t_{\text{rm}}(y)$	Cluster
V615 Per	2×10^7	0.61×10^7	2.92×10^7	0.0836	0.712	9.96×10^7	NGC 869
V618 Per	2×10^7	0.61×10^7	—	—	—	—	NGC 869
V453 Cyg	1.05×10^7	0.10×10^7	9.76×10^6	0.0193	0.018	0.02×10^7	NGC 6871
V1229 Tau	1.93×10^8	0.17×10^8	1.24×10^8	0.0045	0.027	0.19×10^8	Pleiades
V578 Mon	3.50×10^6	0.14×10^6	—	—	—	—	NGC 2244
V906 Sco	2.52×10^8	0.21×10^8	2.53×10^8	0.0241	0.069	0.17×10^8	NGC 6475
V497 Cep	2.30×10^7	0.48×10^7	2.17×10^7	0.0209	0.053	0.26×10^7	NGC 7160
V381 Car	1.05×10^7	0.11×10^7	1.05×10^7	0.0800	0.030	0.04×10^7	NGC 3293
V392 Car	1.23×10^8	0.15×10^8	1.41×10^8	0.0089	0.472	4.86×10^8	NGC 2516
V1034 Sco	5.51×10^6	0.42×10^6	5.36×10^6	0.0080	0.016	0.16×10^6	NGC 6231
DW Car	5.22×10^6	0.30×10^6	4.88×10^6	0.0229	0.188	2.93×10^6	Cr 228
GV Car	3.22×10^8	0.61×10^8	3.21×10^8	0.0406	0.064	0.27×10^8	NGC 3532

- [3] Asplund, M., Grevesse, N. & Sauval, A.J., 2005, in Bash, F.N., Barnes, T.G., eds., ASP Conf. Ser. 336, Cosmic Abundances as Records of Stellar Evolution and Nucleosynthesis, Astron. Soc. Pac., San Francisco, p.25 (AGS2005)
- [4] Bouzid, M.Y., Sterken, C. & Pribulla, T., 2005 A&A, 437, 769
- [5] Clausen, J.V., Garcia, J.M., Gimenez, A., Helt, B.E., Jensen, K.S., Suso, J. & Vaz, L.P.R., 1996, A&A, 308, 151
- [6] Debernardi, Y. & North, P., 2001, A&A, 374, 204
- [7] del Peloso, E.F., da Silva, L., Porto de Mello, G.F. & Arany-Prado, L.I. 2005, A&A, 440, 1153
- [8] Eggenberger, P., Miglio, A., Carrier, F., Fernandes, J. & Santos, N.C. 2008, A&A, 482, 631
- [9] Freyhammer, L.M., Hensberge, H., Sterken, C., Pavlovski, K., Smette, A. & Ilijic, S., 2005, A&A, 429, 631
- [10] Freyhammer, L.M., Hensberge, H., Sterken, C., De Cat, P. & Aerts, C., 2006, Mem. S.A.It., 77, 334
- [11] Garcia, E., Stassun, K.G., Hebb, L. & Heiser, A., 2010, AAS, 21541940
- [12] Girardi, L., Bertelli, G., Bressan, A., Chiosi, C., Groenewegen, M. A. T., Marigo, P., Salasnich, B. & Weiss, A., 2002, A&A, 391, 195
- [13] Groenewegen, M.A.T., Decin, L., Salaris, M. & De Cat, P., 2007, A&A, 463, 579
- [14] Hensberge, H., Pavlovski, K. & Verschueren, W., 2000, A&A, 358, 553
- [15] Kharchenko, N.V., Piskunov, A.E., Röser, S., Schilbach, E. & Scholz, R.-D., 2005, A&A, 438, 1163
- [16] Lastennet, E. & Valls-Gabaud, D., 2002, A&A, 396, 551
- [17] Mamajek, E.E. & Hillenbrand, L.A. 2008, ApJ, 687, 1264
- [18] Meynet, G. & Maeder, A., 2000, A&A, 361, 101
- [19] Munari, U., Dallaporta, S., Siviero, A., Soubiran, C., Fiorucci, M. & Girard, P., 2004, A&A, 418, 31
- [20] Pavlovski, K. & Hensberge, H., 2005, A&A, 439, 309
- [21] Pavlovski, K., Southworth, J., 2009, MNRAS, 394, 1519
- [22] Pols, O.R., Tout, C.A., Schroder, K.-P., Eggleton, P.P. & Manners, J., 1997, MNRAS, 289, 869
- [23] Schaller, G., Schaerer, D., Meynet, G. & Maeder, A., 1992, A&AS, 96, 269
- [24] Southworth, J., Maxted, P.F.L. & Smalley, B., 2004a, MNRAS, 349, 547
- [25] Southworth, J., Maxted, P.F.L. & Smalley, B., 2004b, MNRAS, 351, 1277
- [26] Southworth, J., Maxted, P.F.L. & Smalley, B., 2005, A&A, 429, 645
- [27] Southworth, J. & Clausen, J.V., 2006, Ap&SS, 304, 199
- [28] Southworth, J. & Clausen, J.V., 2007, A&A, 461, 1077
- [29] Torres, G., Andersen, J. & Gimenez, A., 2010, A&ARv, 18, 67
- [30] Williams, S. J., 2009, 2009, AJ, 137, 3222
- [31] Yakut K., Tarasov A.E., İbanoğlu C., Harmanec P., Kalomeni B., Holmgren D.E., Bozic H. & Eenens P., 2003, A&A, 405, 1087
- [32] Yıldız, M. & Kızıloğlu, N., 1997, A&A, 362, 187
- [33] Yıldız, M., 2003, A&A, 409, 689
- [34] Yıldız, M., 2005, MNRAS, 363, 967
- [35] Yıldız, M., Yakut, K., Bakış, H. & Noels, A., 2006, MNRAS, 368, 1941
- [36] Yıldız M., 2007, MNRAS, 374, 1264
- [37] Yıldız M., 2008, MNRAS, 388, 1143